

|  |  |
|--|--|
| <p><b>1.</b> Are the following relations functions?</p> <p><b>(a)</b> <math>\{(1, 2), (1, 3), (2, 3)\}</math></p> <p>No. (1, 2) and (1, 3) pair 1 with 2 and 3.</p> <p><b>(b)</b> <math>\{(x, y)   y = 2x^2\}</math></p> <p>Yes. Every <math>x</math> value is paired with exactly one <math>y</math> value.</p> | <p><b>2.</b> Are the following functions one-to-one?</p> <p><b>(a)</b> <math>\{(1, 2), (2, 3), (4, 4)\}</math></p> <p>Yes. Every <math>y</math> value is paired with exactly one <math>x</math> value.</p> <p><b>(b)</b> <math>\{(x, y)   y = x^2 + 1\}</math></p> <p>No. When <math>y = 2</math>, <math>x = 1</math> and <math>x = -1</math>.</p> |
| <p><b>3.</b> Find the inverse function.</p> $f(x) = 2x - 9$ $y = 2x - 9$ $x = 2y - 9$ $x + 0 = 2y - 9$ $\frac{+9}{+9} \quad \frac{+9}{+9}$ $x + 9 = 2y + 0$ $\frac{x + 9}{2} = \frac{2y}{2}$ $f^{-1}(x) = \frac{x + 9}{2}$   | <p><b>4.</b> Find the inverse function.</p> $f(x) = \frac{x + 2}{x}$ $y = \frac{x + 2}{x}$ $x = \frac{y + 2}{y}$ $y \cdot x = y \cdot \frac{y + 2}{y}$ $xy = y + 2$ $\frac{-y}{xy} = \frac{-y}{y + 2}$ $y(x - 1) = 2$ $\frac{y(x - 1)}{x - 1} = \frac{2}{x - 1}$ $f^{-1}(x) = \frac{2}{x - 1}$   |

5. Find the ending balance in a savings account if the initial principal, \$12,000, was invested at a rate of 6%, compounded monthly, for 10 years.

$$A = P \left( 1 + \frac{r}{n} \right)^{nt}$$

$$P = 12,000; r = 0.06; n = 12; t = 10$$

$$A = 12000 \left( 1 + \frac{.06}{12} \right)^{12 \cdot 10}$$

$$A = 12000(1 + 0.005)^{12 \cdot 10}$$

$$A = 12000(1.005)^{120}$$

$$A \approx \$21,832.76$$

6. Find the ending balance in a savings account if the initial principal, \$12,000, was invested at a rate of 6%, compounded continuously, for 10 years.

$$A = Pe^{rt}$$

$$P = 12,000; r = 0.06; t = 10$$

$$A = 12000e^{0.06 \cdot 10}$$

$$A = 12000e^{0.6}$$

$$A \approx \$21865.43$$

7. Solve.

$$25^{4x} = 5$$

$$(5^2)^{4x} = 5$$

$$5^{8x} = 5^1$$

$$8x = 1$$

$$\frac{8x}{8} = \frac{1}{8}$$

$$x = \frac{1}{8}$$

8. Solve.

$$16^{x+1} = 8$$

$$(2^4)^{x+1} = 2^3$$

$$2^{4(x+1)} = 2^3$$

$$2^{4x+4} = 2^3$$

$$4x + 4 = 3$$

$$\frac{-4}{-4} \quad \frac{-4}{-4}$$

$$4x + 0 = -1$$

$$\frac{4x}{4} = \frac{-1}{4}$$

$$x = -\frac{1}{4}$$

9. Solve.

$$\begin{aligned}
 9^{x+2} &= 3^{x-1} \\
 (3^2)^{x+2} &= 3^{x-1} \\
 3^{2(x+2)} &= 3^{x-1} \\
 3^{2x+4} &= 3^{x-1} \\
 2x+4 &= x-1 \\
 \frac{-x}{x+4} &= \frac{-x}{0-1} \\
 \frac{-4}{x+0} &= \frac{-4}{-1-1} \\
 x &= -5
 \end{aligned}$$

10. Solve.

$$\begin{aligned}
 \frac{1}{4^x} &= 8^{2x+1} \\
 \frac{1}{(2^2)^x} &= (2^3)^{2x+1} \\
 \frac{1}{2^{2x}} &= 2^{3(2x+1)} \\
 2^{-2x} &= 2^{6x+3} \\
 -2x &= 6x+3 \\
 \frac{-6x}{-8x} &= \frac{-6x}{0+3} \\
 \frac{-8x}{-8} &= \frac{3}{-8} \\
 x &= -\frac{3}{8}
 \end{aligned}$$

11. The population of aphids on a rose plant is given by the following formula:

$$P = 80e^{0.17t}$$

where  $t$  is time (in weeks) since the plant was inspected. Find the aphid population at 2 weeks.

$$\begin{aligned}
 P &= 80e^{0.17t} \\
 P &= 80e^{0.17 \cdot 2} \\
 P &= 80e^{0.34} \\
 P &\approx 112 \text{ aphids}
 \end{aligned}$$

12. What amount should be invested at 4% compounded continuously in order to have an accumulated savings of \$50,000 in 18 years?

$$\begin{aligned}
 A &= Pe^{rt} \\
 A &= 50000; \quad r = 0.04; \quad t = 18 \\
 50000 &= Pe^{0.04 \cdot 18} \\
 50000 &= Pe^{0.72} \\
 \frac{50000}{e^{0.72}} &= \frac{Pe^{0.72}}{e^{0.72}} \\
 \frac{50000}{e^{0.72}} &= P \\
 P &\approx \$24,337.61
 \end{aligned}$$

|  |  |
|--|--|
| <p><b>13.</b> Write the exponential equations in logarithmic form</p> <p>(a) <math>3^4 = 81</math><br/><math>\log_3(81) = 4</math></p> <p>(b) <math>12^0 = 1</math><br/><math>\log_{12}(1) = 0</math></p>  | <p><b>14.</b> Write the following logarithmic equations in exponential form</p> <p>(a) <math>\log_5(125) = 3</math><br/><math>5^3 = 125</math></p> <p>(b) <math>\ln(5) = x</math><br/><math>e^x = 5</math></p>   |
| <p><b>15.</b> Evaluate</p> <p>(a) <math>\log_5(625)</math><br/><math>\log_5(625) = x</math><br/><math>5^x = 625</math><br/><math>5^x = 5^4</math><br/><math>x = 4</math><br/><math>\log_5(625) = 4</math></p> <p>(b) <math>\ln e</math><br/><math>\ln e = x</math><br/><math>e^x = e</math><br/><math>e^x = e^1</math><br/><math>x = 1</math><br/><math>\ln e = 1</math></p> | <p><b>16.</b> Use a calculator to evaluate the following. Round your answers to the nearest hundredth (x.xx)</p> <p>(a) <math>\log(4.5)</math><br/><math>\log(4.5) \approx 0.65</math></p> <p>(b) <math>\ln(4.5)</math><br/><math>\ln(4.5) \approx 1.50</math></p> |

17. Use the properties of logarithms to rewrite the expression as logarithms of single variables or numbers. Simplify if possible.

$$\log_m\left(\frac{5^2}{m}\right)$$

$$= \log_m(5^2) - \log_m(m)$$

$$= 2\log_m(5) - 1$$

18. Use the properties of logarithms to rewrite the expression as a single logarithm.

$$\frac{1}{2}\log_m(5) + 3\log_m(x)$$

$$= \log_m(5^{\frac{1}{2}}) + \log_m(x^3)$$

$$= \log_m(\sqrt{5}) + \log_m(x^3)$$

$$= \log_m(x^3 \sqrt{5})$$

19. Solve (to nearest hundredth x.xx)

(a)  $5^x = 10$

$$\log 5^x = \log 10$$

$$x \cdot \log 5 = 1$$

$$\frac{x \log 5}{\log 5} = \frac{1}{\log 5}$$

$$x = \frac{1}{\log 5}$$

$$x \approx 1.43$$

(b)  $e^x = 10$

$$\ln e^x = \ln 10$$

$$x \cdot \ln e = \ln 10$$

$$x \cdot 1 = \ln 10$$

$$x = \ln 10$$

$$x \approx 2.30$$

20. Solve

$$\log_3(x) + \log_3(x - 2) = \log_3(15)$$

$$\log_3(x)(x - 2) = \log_3(15)$$

$$\log_3(x^2 - 2x) = \log_3(15)$$

$$x^2 - 2x = 15$$

$$x^2 - 2x + 0 = 15$$

$$x^2 - 2x - 15 = 0$$

$$(x + 3)(x - 5) = 0$$

$$x + 3 = 0 \quad \text{or} \quad x - 5 = 0$$

$$x + 0 = -3 \quad \text{or} \quad x + 0 = 5$$

$$x = -3 \quad \text{or} \quad x = 5$$

-3 is not an allowable value (it's a negative argument)

Solution set:  $\{5\}$